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A First-Level Analysis of The Adsorption Mechanism of Esters of Racemic and Meso-2,3-dibromobutane 1,4-dioic Acids on Silica<br>M. Palamareva; I. Kozekov ${ }^{\text {a }}$<br>${ }^{\text {a }}$ Department of Chemistry, University of Sofia 1 James Bourchier Avenue Sofia, Bulgaria

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# A FIRST-LEVEL ANALYSIS OF THE ADSORPTION MECHANISM OF ESTERS OF RACEMIC AND MESO-2,3-DIBROMOBUTANE-1,4-DIOIC ACIDS ON SILICA 

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#### Abstract

The thin-layer chromatographic (TLC) retention of eighteen diastereoisomers of type $\mathrm{RO}_{2} \mathrm{C}-\mathrm{CH}(\mathrm{Br})-\mathrm{CH}(\mathrm{Br})-\mathrm{CO}_{2} \mathrm{R}$ on silica was studied with 20 computer-selected on the basis of Snyder theory mobile phases having strength, $\varepsilon$, in the range 0.215 0.305 and significantly greater variation in localization. $m$, and polarity. $P^{\prime}$.

A theoretical analysis, using Soczewiñski method, the $\varepsilon$ values of the mobile phases used and the stereochemical particularities of the compounds, showed that the two ester groups are the main adsorbing groups, shielded by the bromine atoms. which accounts for the relative retention: racemate $>$ meso found in all cases studied. Two mobile phases of intermediate $m$ values lead to best separation of all diastereoisomeric pairs studied.




Z


racemate (RR|SS)
$R=\left[\begin{array}{l}\mathrm{CH}_{3}, \mathrm{C}_{2} \mathrm{H}_{5}, \mathrm{n}-\mathrm{C}_{3} \mathrm{H}_{7}, \text { iso }-\mathrm{C}_{3} \mathrm{H}_{7}, \\ \mathrm{n}-\mathrm{C}_{4} \mathrm{H}_{9}, \text { sec. }-\mathrm{C}_{4} \mathrm{H}_{9}, \text { iso }-\mathrm{C}_{4} \mathrm{H}_{9}, \\ \mathrm{n}-\mathrm{C}_{5} \mathrm{H}_{11}, \\ \text { iso }-\mathrm{C}_{5} \mathrm{H}_{11}\end{array}\right.$

Figure 1. Types of the diastereoisomers studied recently ${ }^{8}$ and in this paper. One of the enantiomers is represented for the racemate.

## INTRODUCTION

In a series of papers, ${ }^{1}$ we have reported the TLC adsorptivity of a vast number of conformationally flexible threo-erythro and cis-trans diastereoisomers and rigid Z-E diastereoisomers on, mainly, silica or alumina, with numerous mobile phases. The retention, relative retention and separation of the diastereoisomers have been treated in terms of Snyder theory, ${ }^{2-4}$ the Soczewiñski method ${ }^{5}$ and the Hammett equation. ${ }^{6.7}$ Recently, we have studied ${ }^{8}$ TLC on silica, of diastereoisomers of type a with an increasing size of group R as a simple case of conformationally rigid diastereoisomers possessing only two equal substituents (see Figure 1).

This paper reports the TLC adsorptivity of the related, but conformationally flexible, diastereoisomers of type $\mathbf{b}$, containing two bromine atoms instead of the double bond, enabling us to further compare the role of conformational effects. The mobile phases used were selected on the basis of Snyder theory by a computer program ${ }^{9}$ whose general validity in this respect has been recently summarised. ${ }^{10}$ The discussion of the data obtained includes the application of the Soczewiñski method and a first-level analysis of the adsorption mechanism by a newly proposed procedure. ${ }^{11}$

## THEORY

The conversion of the experimental $R_{F}$ to the TLC retention, $R_{M}$, and separation. $\alpha$. was done by the following equations:

$$
\begin{align*}
& R_{M}=\log k^{\prime}=\log \left(1 / R_{F}-1\right)  \tag{1}\\
& \log \alpha=R_{M \text { (racernate })}-R_{M(\text { meso })} \tag{2}
\end{align*}
$$

where $k^{\prime}$ is the HPLC retention and the subscripts to $R_{M}$ in the last equation show the configuration of the compound. According to Eq. 2, positive values of $\log \alpha$ correspond to relative retention racemate $>$ meso and vice versa. In addition, a greater absolute $\log \alpha$ value indicates a better separation of the corresponding diastereoisomeric pair.

For the case of retention, $R_{M}$, of a sample with mobile phases composed of a non-polar or weakly polar solvent A and a polar solvent B , Soczewiñski ${ }^{5}$ derived the following equation:

$$
\begin{equation*}
R_{M}=R_{M(B)}-n \log N_{B} \tag{3}
\end{equation*}
$$

where $N_{B}$ is the molar fraction of solvent $\mathrm{B}, R_{M(B)}$ is the retention when the solvent is pure B and $n$ is the slope of the linear plot. For a given set of mobile phases, $n$ is proportional to the area of solute molecule under adsorption. ${ }^{12,13}$

According to Snyder theory ${ }^{2-4}$ mobile phases are characterised by strength, $\varepsilon$, proportional to the dimensionless Gibbs energy ( $\Delta G^{\circ} / R T \ln 10$ ) of adsorption of the mobile phase, localization, $m$, measuring the specific interactions adsorbent-composing solvents and polarity, $P^{\prime}$, measuring the interactions sample (solute)-composing solvents ( $c f .$, ref. 10). The greater the $\varepsilon$ value, the weaker is the sample retention; $m$ and $P^{\prime}$ tune the selectivity as measured by $\log \alpha$ of solute pairs and strength, respectively.

The dimensionless Gibbs energy of adsorption, $Q_{i}$, of a solute group $i$ when $\varepsilon>0$ is expressed by

$$
\begin{equation*}
Q_{i}=Q_{i}^{o}-\varepsilon a_{i} \tag{4}
\end{equation*}
$$

where $Q_{i}{ }^{\circ}$ refers to the case when pentane is the mobile phase having $\varepsilon=0$ and $a_{i}$ is the relative effective area of group $i$ under adsorption. Adsorption of group $i$ is possible if

$$
\begin{equation*}
Q_{i}>0 \tag{5}
\end{equation*}
$$

$Q_{i}{ }^{\circ}$ and, therefore, $Q_{i}$ refer to the case where group $i$ is substantially free from interactions with other solute groups. The greater $Q_{i}$, the stronger is the adsorption of group $i$.

## Table 1

## Data for the Mp's or Bp's and Chemical Shift, $\delta$, of the Proton next to

 Bromine in ${ }^{\mathbf{1}} \mathrm{H}$-NMR Spectra of the Compounds 1-18 Studied of Type b| $\mathbf{R}$ | Configuration | No. | mp ${ }^{\circ} \mathrm{C}$ | bp ${ }^{\circ} \mathrm{C}$ | $\delta_{\text {CHBr }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{3}$ | racemate | 1 | 42-43 |  | 4.75 |
|  | meso | 2 | 60-61 |  | 4.60 |
| $\mathrm{CH}_{2} \mathrm{CH}_{3}$ | racemate | 3 |  | 137-138/12 | 4.75 |
|  | meso | 4 | 56-58 |  | 4.60 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | racemate | 5 |  | 155-160/12 | 4.78 |
|  | meso | 6 |  | 165-166/12 | 4.70 |
| $\mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | racemate | 7 |  | 138-140/12 | 4.68 |
|  | meso | 8 | 62-63 |  | 4.63 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | racemate | 9 |  | 178-182/12 | 4.73 |
|  | meso | 10 |  | 186-188/12 | 4.65 |
| $\mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2} \mathrm{CH}_{3}$ | racemate | 11 |  | 83-85/0.04 | 4.70 |
|  | meso | 12 |  | 170-172/12 | 4.60 |
| $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | racemate | 13 |  | 90-91/0.03 | 4.73 |
|  | meso | 14 |  | 95-96/0.02 | 4.68 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | racemate | 15 |  | 117-118/0.10 | 4.73 |
|  | meso | 16 |  | 109-110/0.03 | 4.65 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | racemate | 17 |  | 102-103/0.03 | 4.75 |
|  | meso | 18 |  | 113-114/0.03 | 4.70 |

The mp's are of samples recrystallized from ethanol.
The bp's were measured under vacuum given in mm Hg .
The $\delta$ values are in ppm .
The signal for the CHBr proton is a singlet. Its chemical shift is in a higher field for any meso isomer.

The procedure proposed recently by us ${ }^{11}$ for a first-level analysis of the adsorption mechanism is based on calculation of $Q_{i}$ of all groups $i$ participating in the solute structure under conditions used and discussion of the possible electronic and steric interactions between the adsorbing and non-adsorbing groups $i$.

## EXPERIMENTAL

Compounds $\mathbf{1 - 1 8}$ of type $b$ were prepared in good to high yields by the following stereospecific reactions: (a) addition of bromine to maleic anhydride and following esterification gave the racemic compounds and (b) addition of bromine to the corresponding ester of fumaric acid resulted in the meso compounds.

The ${ }^{1} \mathrm{H}$-NMR spectra of compounds $1-18$ were measured on a TESLA 80 MHz spectrometer in acetone solutions with TMS as internal standard. Compounds $1-5,8,9$ and 18 are known. ${ }^{14-19}$

TLC was performed on silica 60 DG (Readel de Haen, Germany) using the procedure given in ref. 20. The solvents were of analytical-reagent grade. The $R_{F}$ values were arithmetic means of four to six measurements, showing a reproducibility of $\pm 0.025$. The computer program ${ }^{9}$ used was LSChrom Ver. 2 for Windows.

## RESULTS AND DISCUSSION

The mp's or bp's and data from ${ }^{1} H-N M R$ spectra of compounds $\mathbf{1 - 1 8}$ are given in Table 1. Table 2 summarizes the mobile phases $1-20$ used with their computer - calculated ${ }^{9}$ values of $\varepsilon, m$ and $P^{\prime}$, including $N_{B}$ for the binary mobile phases. The computer choice of mobile phases $1-18$ was similar to that described in ref. 10. The mobile phases are composed of two to four solvents comprising eight non-localizing or weakly-localizing solvents and the localizing diethyl ether, ethyl acetate, methyl tert-butyl ether, acetonitrile and tetrahydrofurane. ${ }^{4}$ Mobile phases 1-10 and mobile phases 11-15 have equal $\varepsilon$ of 0.253 and 0.240 , respectively. Mobile phases 5 and $16-20$ are composed of hexane (solvent A ) and ethyl acetate (solvent B ) in different ratios, showing molar fraction, $N_{B}$. from 0.026 to 0.201 and $\varepsilon$ in the range $0.215-0.303$. Thus, all mobile phases used have minimum and maximum $\varepsilon$ of 0.215 and 0.303 , respectively. They show greater variations in $m$ and $P^{\prime}$, namely $-0.15 \leq m \leq$ 0.95 and $0.19 \leq P^{\prime} \leq 2.75$.

Table 3 includes the data for the experimental $R_{F}$ values obtained in TLC on silica of compounds $1-18$ with mobile phases 1-20. The values of $\log \alpha$ derived by Eqns. 1 and 2 and their average values are also included. The tuning effect of $P^{\prime}$ on $\varepsilon$ is seen. For instance, mobile phases 9 and 10 with the greatest $P^{\prime}$ when $\varepsilon=0.253$, lead to reduction in retention and higher $R_{F}$. The small difference in $\varepsilon$ of mobile phases 1-10 and 11-15 (0.013) results in
Table 2
Mobile Phases used in TLC on Silica and the Corresponding Computer-Calculated ${ }^{9}$ Values of Strength, $\varepsilon$, Localization,

| Composition (vol \%) | $\mathbf{N}_{\text {B }}$ | $\varepsilon$ | $m$ | $P^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: |
| $90.00: 10.00$ | 0.122 | 0.253 | 0.61 | 0.37 |
| 60.40: 39.60 | 0.516 | 0.253 | 0.14 | 1.45 |
| 44.11:55.89 | 0.721 | 0.253 | 0.10 | 1.78 |
| 97.64 : 2.36 | 0.041 | 0.253 | 0.85 | 0.22 |
| $94.65: 5.35$ | 0.070 | 0.253 | 0.57 | 0.33 |
| 95.85:4.15 | 0.045 | 0.253 | 0.73 | -- |
| 97.97:2.03 | 0.049 | 0.253 | 0.82 | 0.22 |
| 92.61:7.39 | 0.113 | 0.253 | 0.95 | 0.39 |
| 87.24:12.76 | 0.190 | 0.253 | 0.01 | 2.75 |
| 27.99:72.01 | 0.810 | 0.253 | -0.15 | 2.11 |
| 83.72 : $10.00: 6.28$ | -- | 0.240 | 0.54 | 0.17 |
| $85.75: 5.00: 5.00: 4.25$ | -- | 0.240 | 0.46 | 0.20 |
| $77.20: 10.00: 10.00: 2.80$ | -- | 0.240 | 0.34 | 0.43 |
| (continued) |  |  |  |  | $y, P^{\prime}$, including Binary Mobile Phases

Composition (vol \%)
$90.00: 10.00$
$60.40: 39.60$
$44.11: 55.89$
$97.64: 2.36$
$94.65: 5.35$
$95.85: 4.15$
$97.97: 2.03$
$92.61: 7.39$
$87.24: 12.76$
$27.99: 72.01$
$83.72: 10.00$
$85.75: 5.00$ :
(continued)
Table 2 (continued)
Mobile Phases used in TLC on Silica and the Corresponding Computer-Calculated ${ }^{9}$ Values of Strength, $\varepsilon$, Localization,

| $\mathbf{N}_{B}$ | $\boldsymbol{\varepsilon}$ | $\boldsymbol{m}$ | $\boldsymbol{P}^{\prime}$ |
| :---: | :---: | :---: | :---: |
| -- | 0.240 | 0.17 | 0.69 |
| -- | 0.240 | 0.04 | 0.94 |
|  |  |  |  |
| 0.026 | 0.215 | 0.54 | 0.19 |
| 0.050 | 0.240 | 0.56 | 0.27 |
| 0.103 | 0.270 | 0.58 | 0.44 |
| 0.153 | 0.288 | 0.58 | 0.62 |
| 0.201 | 0.303 | 0.59 | 0.79 |

Experimental $R_{F}$ Values and Derived Values of $\log \alpha$ for the Diastereomeric Compounds 1-18 of Type $h$
20 Avg.
$\begin{array}{llllllllllllllllllll}0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 \\ 0.30 & 0.48 \\ 0.45 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76\end{array} 0.46$
$\begin{array}{lllllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 045 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.65 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.5 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56\end{array}$
$\begin{array}{llllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.1 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 1.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.5 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{llllllllllllllllllllllll}0.41 & 1.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.31 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.5 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.5 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{lllllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 1.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.5 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{llllllllllllllllllllll}0.41 & 1.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.1 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{lllllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 045 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.65 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.5 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56\end{array}$
$\begin{array}{llllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.1 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 1.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.5 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{llllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.5 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 1.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
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$\begin{array}{llllllllllllllllllllll}0.41 & 1.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.5 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.1 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
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640.28
$\begin{array}{llllllllllllllllllllllll}0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.34 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.46 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.644 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.6 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
13
$\begin{array}{llllllllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.5 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.5 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{lllllllllllllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.5 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.51 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{lllllllllllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.55 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.5 & 0.24 & 0.37 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.5 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$

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110.460 .550 .29
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$\begin{array}{lllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.5 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.5 & 0.24 & 0.3 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
$\begin{array}{lllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.5 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.5 & 0.24 & 0.3 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$
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$\begin{array}{llllllllllllllllllllllllll}0.27 & 0.26 & 0.42 & 0.18 & 0.24 & 0.21 & 0.08 & 0.34 & 0.40 & 0.56 & 0.26 & 0.20 & 0.28 & 0.26 & 0.29 & 0.11 & 0.19 & 0.31 & 0.46 & 0.55 & 0.29 \\ 0.41 & 0.41 & 0.51 & 0.27 & 0.35 & 0.29 & 0.13 & 0.45 & 0.51 & 0.62 & 0.37 & 0.31 & 0.39 & 0.37 & 0.39 & 0.18 & 0.28 & 0.42 & 0.58 & 0.67 & 0.40 \\ 0.36 & 0.42 & 0.50 & 0.26 & 0.34 & 0.26 & 0.11 & 0.46 & 0.47 & 0.61 & 0.38 & 0.26 & 0.36 & 0.33 & 0.36 & 0.16 & 0.25 & 0.40 & 0.58 & 0.67 & 0.38 \\ 0.50 & 0.48 & 0.55 & 0.33 & 0.42 & 0.33 & 0.16 & 0.53 & 0.54 & 0.67 & 0.48 & 0.38 & 0.46 & 0.44 & 0.47 & 0.21 & 0.33 & 0.49 & 0.67 & 0.76 & 0.46 \\ 0.45 & 0.50 & 0.55 & 0.31 & 0.40 & 0.31 & 0.12 & 0.54 & 0.5 & 0.69 & 0.48 & 0.32 & 0.45 & 0.43 & 0.45 & 0.18 & 0.29 & 0.47 & 0.66 & 0.77 & 0.45 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.59 & 0.60 & 0.72 & 0.54 & 0.43 & 0.51 & 0.49 & 0.5 & 0.24 & 0.3 & 0.53 & 0.73 & 0.84 & 0.51 \\ 0.47 & 0.50 & 0.54 & 0.31 & 0.42 & 0.31 & 0.13 & 0.55 & 0.50 & 0.66 & 0.44 & 0.33 & 0.42 & 0.39 & 0.41 & 0.20 & 0.31 & 0.48 & 0.68 & 0.78 & 0.44 \\ 0.56 & 0.56 & 0.59 & 0.38 & 0.48 & 0.37 & 0.18 & 0.60 & 0.56 & 0.71 & 0.53 & 0.42 & 0.50 & 0.49 & 0.50 & 0.25 & 0.37 & 0.55 & 0.74 & 0.83 & 0.51 \\ 0.50 & 0.60 & 0.62 & 0.37 & 0.45 & 0.35 & 0.18 & 0.60 & 0.64 & 0.75 & 0.50 & 0.38 & 0.49 & 0.48 & 0.51 & 0.21 & 0.33 & 0.52 & 0.73 & 0.84 & 0.50 \\ 0.61 & 0.61 & 0.62 & 0.40 & 0.51 & 0.38 & 0.21 & 0.63 & 0.65 & 0.78 & 0.58 & 0.47 & 0.54 & 0.53 & 0.55 & 0.26 & 0.40 & 0.58 & 0.79 & 0.88 & 0.55 \\ 0.56 & 0.63 & 0.58 & 0.41 & 0.48 & 0.42 & 0.25 & 0.58 & 0.58 & 0.72 & 0.53 & 0.47 & 0.51 & 0.47 & 0.51 & 0.23 & 0.35 & 0.56 & 0.78 & 0.87 & 0.52 \\ 0.61 & 0.64 & 0.58 & 0.44 & 0.52 & 0.46 & 0.28 & 0.61 & 0.60 & 0.74 & 0.60 & 0.55 & 0.57 & 0.52 & 0.59 & 0.28 & 0.40 & 0.61 & 0.82 & 0.89 & 0.57 \\ 0.53 & 0.63 & 0.58 & 0.38 & 0.48 & 0.42 & 0.23 & 0.56 & 0.60 & 0.75 & 0.53 & 0.47 & 0.54 & 0.49 & 0.55 & 0.20 & 0.32 & 0.55 & 0.79 & 0.87 & 0.52 \\ 0.63 & 0.65 & 0.60 & 0.45 & 0.53 & 0.47 & 0.28 & 0.61 & 0.65 & 0.77 & 0.60 & 0.54 & 0.58 & 0.54 & 0.59 & 0.26 & 0.39 & 0.60 & 0.84 & 0.90 & 0.57 \\ 0.53 & 0.67 & 0.59 & 0.39 & 0.47 & 0.45 & 0.24 & 0.60 & 0.68 & 0.80 & 0.55 & 0.48 & 0.57 & 0.54 & 0.60 & 0.22 & 0.34 & 0.55 & 0.78 & 0.89 & 0.55 \\ 0.64 & 0.70 & 0.61 & 0.46 & 0.55 & 0.51 & 0.33 & 0.65 & 0.69 & 0.80 & 0.63 & 0.57 & 0.62 & 0.57 & 0.64 & 0.27 & 0.40 & 0.61 & 0.84 & 0.91 & 0.60 \\ 0.56 & 0.69 & 0.60 & 0.38 & 0.47 & 0.44 & 0.25 & 0.62 & 0.64 & 0.79 & 0.58 & 0.53 & 0.59 & 0.55 & 0.60 & 0.22 & 0.35 & 0.56 & 0.80 & 0.89 & 0.56 \\ 0.66 & 0.69 & 0.61 & 0.46 & 0.55 & 0.53 & 0.34 & 0.68 & 0.68 & 0.81 & 0.64 & 0.58 & 0.63 & 0.57 & 0.64 & 0.28 & 0.41 & 0.61 & 0.87 & 0.91 & 0.61\end{array}$

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Table 3 (continued)
$\begin{array}{cllllllllllllllllllllll}\mathbf{1 - 2} & 0.27 & 0.30 & 0.16 & 0.23 & 0.23 & 0.19 & 0.24 & 0.20 & 0.19 & 0.11 & 0.22 & 0.25 & 0.22 & 0.22 & 0.19 & 0.25 & 0.22 & 0.21 & 0.21 & 0.22 & 0.22 \\ \mathbf{3 - 4} & 0.25 & 0.11 & 0.09 & 0.15 & 0.15 & 0.15 & 0.19 & 0.12 & 0.12 & 0.11 & 0.18 & 0.24 & 0.18 & 0.20 & 0.20 & 0.14 & 0.17 & 0.16 & 0.17 & 0.19 & 0.16 \\ \mathbf{5 - 6} & 0.19 & 0.10 & 0.07 & 0.13 & 0.14 & 0.12 & 0.21 & 0.09 & 0.09 & 0.06 & 0.10 & 0.20 & 0.10 & 0.11 & 0.10 & 0.16 & 0.16 & 0.10 & 0.14 & 0.20 & 0.13 \\ 7.8 & 0.16 & 0.10 & 0.09 & 0.13 & 0.11 & 0.12 & 0.17 & 0.09 & 0.10 & 0.10 & 0.16 & 0.17 & 0.14 & 0.18 & 0.16 & 0.12 & 0.12 & 0.12 & 0.13 & 0.14 & 0.13 \\ \mathbf{9 - 1 0} & 0.19 & 0.02 & 0.00 & 0.06 & 0.10 & 0.06 & 0.08 & 0.06 & 0.02 & 0.07 & 0.14 & 0.16 & 0.09 & 0.09 & 0.07 & 0.12 & 0.13 & 0.1 & 0.14 & 0.15 & 0.09 \\ \mathbf{1 1 - 1 2} & 0.09 & 0.02 & 0.0 & 0.05 & 0.07 & 0.07 & 0.07 & 0.05 & 0.04 & 0.04 & 0.12 & 0.14 & 0.11 & 0.09 & 0.14 & 0.11 & 0.09 & 0.09 & 0.11 & 0.08 & 0.08 \\ \mathbf{1 3 - 1 4} & 0.18 & 0.04 & 0.04 & 0.13 & 0.09 & 0.09 & 0.11 & 0.09 & 0.09 & 0.05 & 0.12 & 0.12 & 0.07 & 0.09 & 0.07 & 0.15 & 0.13 & 0.09 & 0.14 & 0.03 & 0.10 \\ \mathbf{1 5 - 1 6} & 0.20 & 0.06 & 0.04 & 0.12 & 0.14 & 0.10 & 0.19 & 0.09 & 0.02 & 0.00 & 0.14 & 0.16 & 0.09 & 0.05 & 0.07 & 0.12 & 0.11 & 0.11 & 0.17 & 0.10 & 0.10 \\ 17-18 & 0.18 & 0.00 & 0.02 & 0.14 & 0.14 & 0.16 & 0.19 & 0.11 & 0.08 & 0.05 & 0.11 & 0.09 & 0.07 & 0.04 & 0.07 & 0.14 & 0.11 & 0.09 & 0.22 & 0.10 & 0.11\end{array}$
$\log \alpha \quad 0.19 \quad 0.080 .050 .130 .130 .120 .160 .100 .080 .070 .140 .170 .120 .120 .120 .150 .140 .120 .160 .14$
A: $\mathrm{CH}_{3} ; \mathrm{B}: \mathrm{CH}_{2} \mathrm{CH}_{3} ; \mathrm{C}: \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3} ; \mathrm{D}: \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2} ; \quad \mathrm{E}: \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3} ;$ F: $\mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2} \mathrm{CH}_{3} ; \quad \mathrm{G}: \mathrm{CH} \mathrm{CH}_{2}\left(\mathrm{CH}_{3}\right) ; \quad \mathrm{H}: \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$; 1: $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$. For composition of mobile phases, see Table 1. The $\log \alpha$ values were calculated from $\mathrm{R}_{\mathrm{F}}$ by Eq. 1 and 2 . The $\log \alpha$ values are average values of $\log \alpha$ for all diastereomeric pairs obtained with a given mobile phase.
practically equal average $R_{F}$ of 0.49 and 0.48 , respectively. Similarly to a previous study, ${ }^{0}$ a linear relationship was found between the average $R_{F}$ values of the individual compounds of a given configuration with mobile phases 1-10 and $11-15$ of equal $\varepsilon$ and the corresponding standard deviations, S.D.. within $R_{F}$. The plots show S.D. in the range $0.003-0.012$. The relative retention racemate $>$ meso was established in all cases studied as seen from the positive $\log \alpha$ independently of the size of group R and the variation in $\varepsilon, m, P^{\prime}$ and $N_{B}$.

Using linear regression analysis, the retention, $R_{M}$, of compounds 1-18 with mobile phases 5 and $16-20$ and the corresponding $N_{B}$ showed a good agreement with Eq. 3. The resulting data for the slope. $n$. intercept, $R_{M /(B)}$. correlation coefficient, $r$. and S.D. are summarised in Table 4.

Table 5 includes literature data ${ }^{2}$ for $Q_{i}{ }^{\circ}, a_{i}$ and calculated by eqn. $4 Q_{i}$ values for the groups $i$ participating in the structure of compounds $\mathbf{1 - 1 8}$ under the conditions used specified by the mobile phases 16 and 20 of minimum and maximum $\varepsilon$, respectively.

## Application of the Soczewiñski Method

The data of Table + show that the Soczewiñski method is applicable to the cases studied showing average $r$ of 0.957 and S.D. of 0.11 . The very close $n$ values for any diastereoisomeric pair support practically equal, within the experimental error, solute areas under adsorption and, therefore, same adsorbing groups for the individual diastereoisomers. For all compounds studied. the absolute $n$ values increase from 1.11 to 1.63 with the increase in the size of group R supporting that the two ester groups are adsorbing in any case. The increase in the area of the ester groups is expected on the basis of their increasing $a_{i}$ values given in Table 5. The values of the slope, $n$, and intercept, $R_{M(B)}$, found determine practically parallel plots for any diastereoisomeric pair showing always a stronger retention for the racemic isomer (see Figure 2), which means that the relative retention racemate $>$ meso cannot change with any variation of $X_{B}$.

## The Relative Retention of Diastereoisomers 1-18 in Terms of a First-level Analysis of the Adsorption Mechanism

As seen from Table 5. the $Q_{i}$ values of bromine and the ester groups are positive under conditions used. Considerable changes in $Q_{i}$ are not expected because both bromine and the ester groups have negative inductive effects and

## Table 4

Data for the Slope, $n$, Intercept, $R_{M(B)}$, Correlation Coefficient, $r$, and S.D. of the Linear Relationships $R_{M}$ vs. $\log N_{B}$ * Found for Compounds of Type b with Mobile Phases 5 and 16-20 Composed of Hexane and Ethyl Acetate

| R C | Configuration | No. | $n$ | $\boldsymbol{R}_{M(B)}$ | $r$ | S.D. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{3}$ | Racemate | 1 | -1.11 | -0.82 | 0.986 | 0.05 |
|  | Meso | 2 | -1.08 | -1.00 | 0.980 | 0.06 |
| $\mathrm{CH}_{2} \mathrm{CH}_{3}$ | Racemate | 3 | -1.15 | -1.06 | 0.978 | 0.06 |
|  | Meso | 4 | -1.19 | -1.26 | 0.975 | 0.07 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Racemate | 5 | -1.31 | -1.35 | 0.973 | 0.08 |
|  | Meso | 6 | -1.32 | -1.51 | 0.951 | 0.11 |
| $\mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | Racemate | 7 | -1.28 | -1.35 | 0.966 | 0.09 |
|  | Meso | 8 | -1.29 | -1.49 | 0.962 | 0.09 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Racemate | 9 | -1.42 | -1.59 | 0.957 | 0.11 |
|  | Meso | 10 | -1.45 | -1.74 | 0.948 | 0.12 |
| $\mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Racemate | 11 | -1.51 | -1.75 | 0.953 | 0.12 |
|  | Meso | 12 | -1.49 | -1.82 | 0.946 | 0.13 |
| $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | Racemate | 13 | -1.61 | -1.84 | 0.960 | 0.12 |
|  | Meso | 14 | -1.60 | -1.95 | 0.944 | 0.14 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | $\mathrm{H}_{3}$ Racemate | 15 | -1.60 | -1.85 | 0.939 | 0.15 |
|  | Meso | 16 | -1.61 | -1.98 | 0.941 | 0.15 |
| $\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$ | Racemate | 17 | -1.62 | -1.89 | 0.945 | 0.14 |
|  | Meso | 18 | -1.63 | -2.04 | 0.930 | 0.16 |
| Average |  |  |  |  | 0.957 | 0.11 |

* $N_{B}$ is the molar fraction of ethyl acetate in mobile phases 5 and 16-20.
resonance between them cannot occur. In addition, the bromine atom is bulkier than $\mathrm{CO}_{2} \mathrm{CH}_{3}$ on the basis of their conformational energies of $1.3 \mathrm{kcal} / \mathrm{mol}$ and $0.9 \mathrm{kcal} / \mathrm{mol},{ }^{21}$ respectively. To evaluate the relative role of the adsorptivity and size of bromine, we calculated the average $R_{F}$ on same silica of the compounds of type a and type b established with hexane-ethyl acetate $92: 8$ ( $\varepsilon=$ 0.270 , mobile phase 19 of ref. 8 and mobile phase 18 of this study). The values found were 0.37 and 0.52 , respectively. This shows that compounds $\mathbf{1 - 1 8}$ of type $\mathbf{b}$ have smaller adsorptivity. The same phenomenon is seen with hexaneethyl acetate $98: 2$ with $\varepsilon=0.215$. Thus, the presence of two bromine atoms


## Table 5

## Data According to Snyder ${ }^{2}$ for the Adsorption Properties on Silica of Groups $i$ Participating in the Compounds Studied

| Group i | $Q_{i}{ }^{\text {b }}$ | $a_{i}$ | $Q_{i}=Q_{i}{ }^{0}-\varepsilon a_{i}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\varepsilon=0.215$ | $\varepsilon=0.303$ |
| Br | 1.94 | 1.80 | 1.55 | 1.39 |
| $\mathrm{CH}_{3}$ | 0.07 | 1.60 | -0.27 | -0.41 |
| $\mathrm{CH}_{2}$ | -0.05 | 0.90 | -0.24 | -0.32 |
| $\mathrm{CO}_{2} \mathrm{CH}_{3}$ | 5.27 | 10.50 | 3.01 | 2.09 |
| $\mathrm{CO}_{2} \mathrm{C}_{2} \mathrm{H}_{5}$ | 5.22 | 11.40 | 2.77 | 1.77 |
| $\mathrm{CO}_{2} \mathrm{C}_{3} \mathrm{H}_{7}-\mathrm{n}$ | 5.17 | 12.30 | 2.53 | 1.44 |
| $\mathrm{CO}_{2} \mathrm{C}_{3} \mathrm{H}_{7}$-iso | 5.29 | 13.00 | 2.50 | 1.35 |
| $\mathrm{CO}_{2} \mathrm{C}_{4} \mathrm{H}_{9}$-n | 5.12 | 13.20 | 2.28 | 1.12 |
| $\mathrm{CO}_{2} \mathrm{C}_{4} \mathrm{H}_{9}-\mathrm{SEC}$ | 5.24 | 13,90 | 2.25 | 1.03 |
| $\mathrm{CO}_{2} \mathrm{C}_{4} \mathrm{H}_{9}$-iso | 5.24 | 13.90 | 2.25 | 1.03 |
| $\mathrm{CO}_{2} \mathrm{C}_{5} \mathrm{H}_{11}-\mathrm{n}$ | 5.07 | 14.10 | 2.04 | 0.80 |
| $\mathrm{CO}_{2} \mathrm{C}_{5} \mathrm{H}_{11}$-iso | 5.19 | 14.80 | 2.01 | 0.71 |

The data for $Q_{i}{ }^{0}$ and $a_{i}$ are taken from ref. 2, p. 200 and p. 264 or calculated by summation of the contribution of the composing fragments. The calculated by Eq. $+Q_{i}$ values refer to the mobile phases of minimum and maximum $\varepsilon$ value used.
with $Q_{i}>0$ does not increase the retention of the compounds of type $\mathbf{b}$ and, therefore, these atoms are expected to have mainly a shielding role. Consequently, adsorption of any two equal ester groups, hindered by the bromine atoms. is the expected simplified adsorption mechanism. The ester groups and. more precisely, their carbonyls having an increased electron density can form hydrogen bonds with the silanol groups. The two-point adsorption occurs via site chelation (see ref. 2, p. 315), i.e., interaction of two adjacent adsorbing groups with a given adsorption site. Conformations suitable for site chelation of the two ester groups are M for the racemates and N for the meso isomers having these two groups in gauche position (see Figure 3). For the racemate. another conformation $\mathrm{M}^{\prime}$ with gauche esters hindered by each of the bromine atoms is not taken into account because the conformational equilibrium is expected to shift to the conformation which will give best adsorption.


Figure 2. $R_{M}$ vs. $\log N_{B}$ plots on the basis of the data of Table 2 and Table 3 for diastereoisomers $1,2,7,8,13,14,17$ and $18 . N_{B}$ is the molar fraction of ethyl acetate in mobile phases 5 and 16-20.

Any racemic compound is expected to show a stronger adsorption because the adsorbing ester groups are not hidered by a bromine atom. On the contrary, such a hindrance is present in the corresponding meso isomer, leading to the relative retention racennate $>$ meso which was found in fact (see Figure 4).

## Separation, $\alpha$, of the Diastereoisomers Studied and Some Comparisons

A fair linear relationship between $\log \alpha$ and $m$ was not observed in this study (cf., refs. 4, 7, 8, 20 and 22). Best separations of all diastereoisomeric pairs studied were obtained with mobile phase 1 and mobile phase 12 , showing average $\log \alpha$ values, $\overline{\log \alpha}$, of 0.19 and 0.17 , respectively (see Table 3 ). These two mobile phases are of intermediate $m$ values ( 0.61 and 0.46 ) and contain the strongly localizing diethyl ether.

meso


1


Figure 3. Conformations of the diastereoisomers studied.

racemate

meso

Figure 4. Schematic illustration of the expected adsorption mechanism on silica for the diastereoisomers studied $\Lambda$ is an adsorption site, probably reactive silanols (see ref. 2, p. 157) suitable for site chelation.

The absence of such a solvent. as in mobile phases $2,3,9$ and 10 , reduces the separation and $\overline{\log \alpha}$ is in the range $0.05-0.08$. Mobile phases $12-15$ are composed of cyclohexane. toluene, benzene and diethyl ether in different ratios. Best separation was established with mobile phase 12 having the greatest $m$ ( 0.46 ) because of the greatest content of diethyl ether.

Let us discuss the average separation of any diastereoisomeric pair obtained with all mobile phases used. According to Table 3, the diastereoisomeric pairs 1-2 and 3-4 with group $R$ equal to methyl and ethyl
show best separation and average $\log \alpha$ of 0.22 and 0.16 . respectively. This probably is due to the stronger adsorptivity of these compounds than that of the remaining compounds with a bulkier group $R$. The opposite is true for the compounds of type $\mathbf{a}$. ${ }^{1}$

Taking into account all $\log \alpha$ values found in ref. 8 and this study, we calculated the corresponding average values for the diastereoisomers of type a and type $b$ being 0.34 and 0.12 , respectively. In our opinion, this reduction in the separation of the diastereoisomers of type $b$ is due to changes both in the structure and the conformational stability of the two types of compounds. The presence of the shorter double bond in the compounds of type a will lead to an increase in the site chelation of the two ester groups in any Z isomer and a greater difference in the retention of the corresponding $E$ isomer where site chelation is not possible because of the rigid conformation. Such an improvement in the site chelations for the two diastereoisomers of type $\mathbf{b}$ cannot occur owing to the presence of the longer $\mathrm{C}(2)-\mathrm{C}(3)$ bond. This assumption is further supported by the fact that the conformationally rigid diastereoisomers of type $\mathrm{C}_{6} \mathrm{H}_{5}-\mathrm{CH}=\mathrm{C}\left(\mathrm{CO}_{2} \mathrm{R}\right)-\mathrm{C}_{6} \mathrm{H}_{5}$, with expected one-point adsorption of the ester group and, therefore, without site chelation, show the same smaller separation ${ }^{11}$ as the compounds of type $b$ studied.

## REFERENCES

1. M. Palamareva, I. Kozekov, I. Jurova, J. Chromatogr. A, 670, 181 (1994); and the references cited therein.
2. L. R. Snyder, Principles of Adsorption Chromatography, Marcel Dekker, Inc., New York, 1968.
3. L. R. Snyder, J. J. Kirkland, Introduction to Modern Liquid Chromatography, Wiley-Interscience, New York, 2nd ed., 1979.
4. L. R. Snyder, in High-performance Liquid Chromatography, Cs. Horváth, ed., Academic press, New York, 1983, Vol. 3, p. 157.
5. E. Soczewiñski, J. Chromatogr., 388, 91 (1987); and the references cited therein.
6. M. Palamareva, S. Chorbadjiev, J. Chem. Soc., Perkin Trans. 2, 961 (1996).
7. M. D. Palamareva. B. J. Kurtev, I. Kavrakova, J. Chromatogr., 545, 161 (1991).
8. M. Palamareva. I. Kozekov. J. Chromatogr., 606, 113 (1992).
9. M. D. Palamareva. H. E. Palamarev, J. Chromatogr., 477, 235 (1989).
10. M. Palamareva. I. Kozekov. J. Liq. Chromatogr., 19. 1483, 1996.
11. M. Palamareva. I. Kozekor, J. Chromatogr., (in press).
12. E. Soczewiñski. W. Golkiewicz, H. Szumilo. J. Chromatogr., 45, 1 (1969).
13. T. Wawrzynowicz. Chem. Anal. (Warsaw). 22, 17 (1977).
14. A. Kekule, Ann. Chem. Pharm., Suppl. 1, 1861, 358.
15. R. Auschutz. Chem. Ber.. 13. 2281 (1879).
16. H. R. Ing. W. H. Perkin. J. Chem. Soc., 125, 1822 (1925).
17. V. D. Yasnopolskii. Zh. Prikl. Khim., 36, 2779 (1963).
18. L. E. Erickson. J. Am. Chem. Soc.. 87. 1867 (1965).
19. E. Larsson. Org. Magn. Resonance, 6, 103 (1974)
20. L. R. Snyder. M. D. Palamareva. B. J. Kurtev, L. Z. Viteva, J. N. Stefanovsky. J. Chromatogr.. 354. 107 (1986).
21. G. Whitesides. J. Sevenair. R. Goetz. J. Amer. Chem. Soc.. 89. 1135 (1967).
22. L. R. Snyder. J. Chromatogr.. 245. 165 (1982).

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